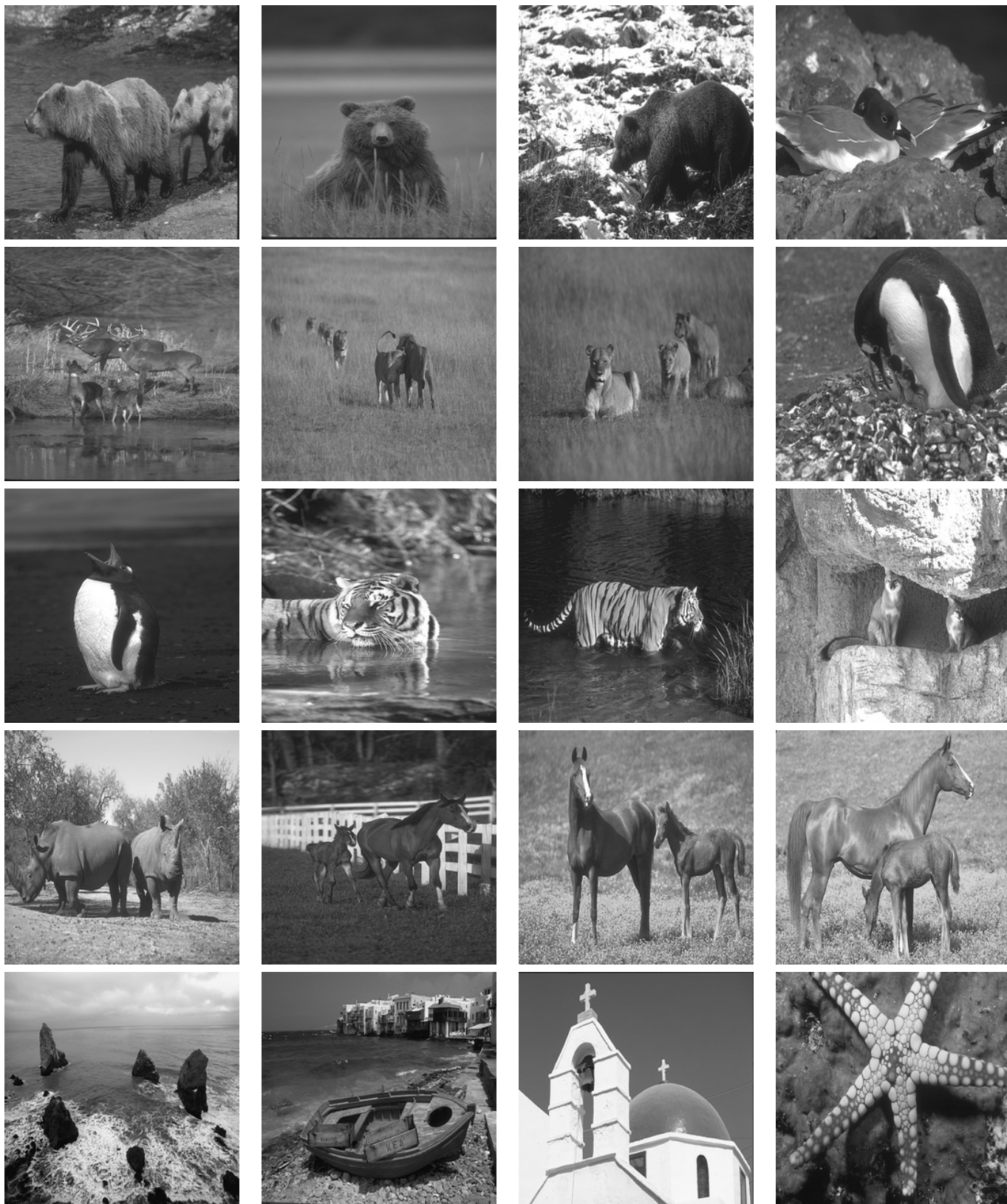


Supplementary material for the paper:  
“Improving Denoising Algorithms via a Multi-Scale Meta-Procedure”  
Paper ID: 100

March 28, 2011

# 1 Training images



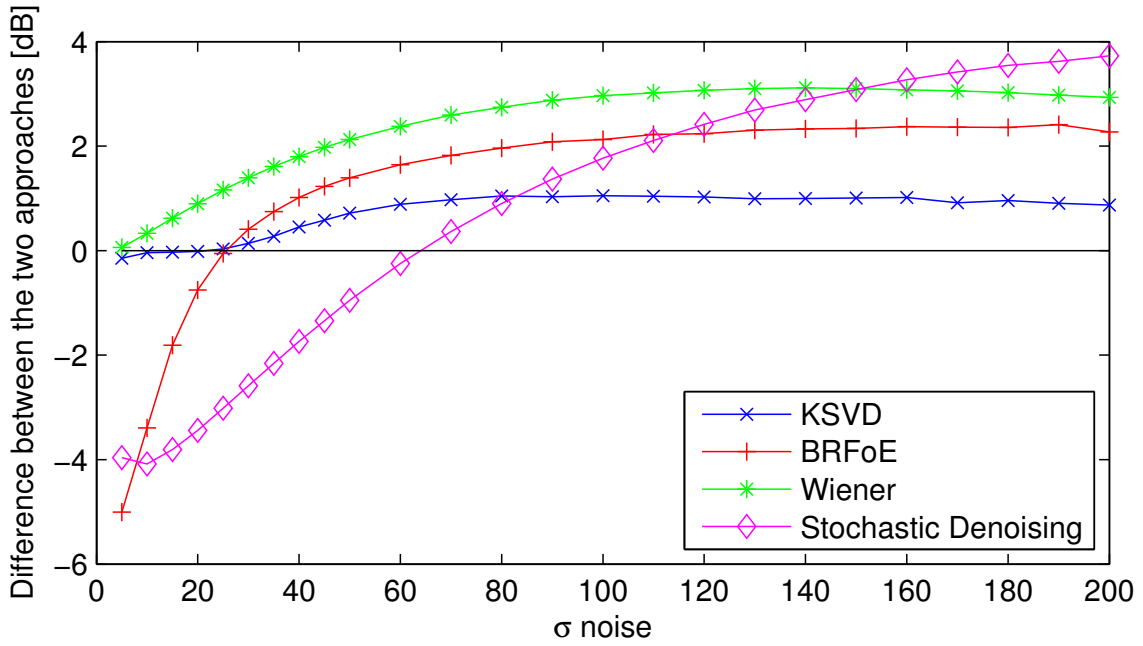
The hyper-parameters of our method were tuned on 20 training images for the Berkeley segmentation. The images are color images, but we worked on black and white versions by averaging the color channels. The images are all either of size  $481 \times 321$  or of size  $321 \times 481$ . We removed one pixel row at the bottom of the images and one pixel column at the right of the images in order to create images of size either  $480 \times 320$  or  $320 \times 480$ . The reason for this was to create images that are multiples of 8 in height and width.

## 2 Test images



The 13 test images are usually named “Barbara”, “Boat”, “Cameraman”, “Couple” (or “Living Room”), “Fingerprint”, “Flintstones”, “Hill” (or “Goldhill”), “House”, “Baboon” (or “Mandrill”), “F16” (or “Fighter Jet”), “Lena”, “Man” (or “Pirate”) and “Peppers”. The images “Cameraman”, “House” and “Peppers” are of size  $256 \times 256$  and all others are of size  $512 \times 512$ . The images “Baboon” and “F16” were color images which we converted to black and white by averaging the color channels, as we did in the training set. All other images are black and white.

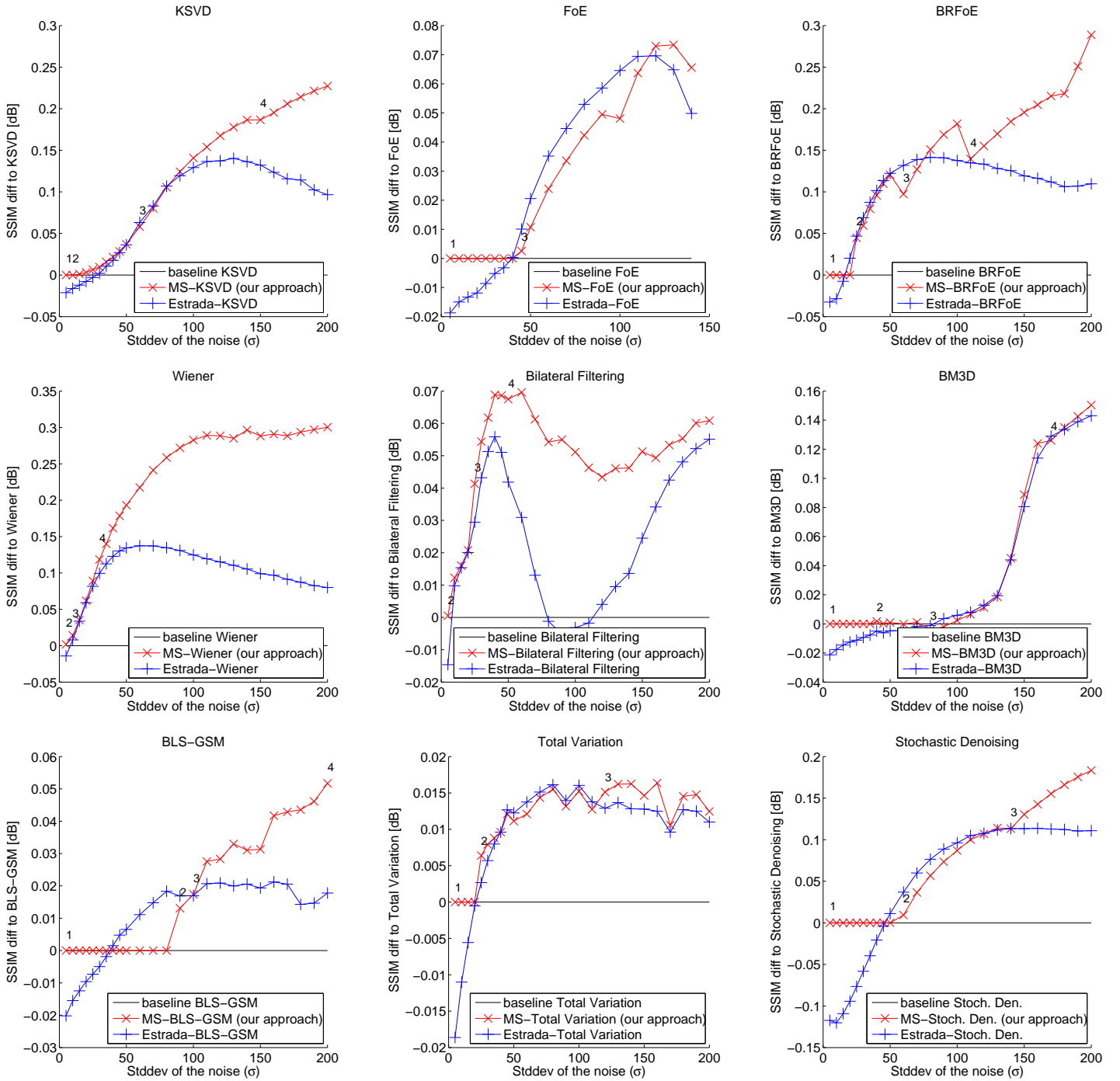
### 3 Notes on how to denoise lower frequencies



In Sec. 3 (“How to denoise lower frequencies”) of the paper, we explained that first down-scaling, then denoising is preferable to first denoising, then down-scaling. However, we provided results on only one image, for one noise setting and using only one denoising algorithm (KSVD).

To gather statistics, we compared the two approaches on the 20 training images for different noise levels. We chose the algorithms KSVD, BRFoE, Wiener and Stochastic denoising. The figure above reports the average difference between the two methods, where a value larger than 0 indicates that it is better to first down-scale, then denoise than vice-versa. So we see that first down-scaling, then denoising is better than the other way around when the noise is strong.

## 4 Improvements in terms of SSIM



The most commonly used measure for image quality is the peak signal to noise ratio (PSNR), which is related to the mean squared error. A shortcoming of the PSNR is that it does not take into account the visual appearance of an image. A measure that attempts to address this issue is the structural similarity index (SSIM) [2]. The SSIM is a value ranging between 0 and 1, where higher values indicate higher similarities.

In the paper, we presented improvements achieved by our approach in terms of PSNR. In the figure above we present the same results in terms of SSIM. We see similar trends as for the PSNR: Our approach outperforms the method proposed by Estrada et al. [1] in most cases. The greatest gains are achieved for the methods KSVD, BRFoE and Wiener.

## 5 Visual comparison for the “Barbara” image



noisy  $\sigma = 200$   
PSNR: 7.59dB, SSIM: 0.074



ground truth



denoised with BM3D  
PSNR: 18.88dB, SSIM: 0.429



denoised with MS-BM3D  
PSNR: 20.96dB, SSIM: 0.591

The images above show the results obtained with BM3D and MS-BM3D (our approach) when noise with  $\sigma = 200$  is added to the “Barbara” image. In the noisy image, one can barely recognize the original image content. BM3D is able to partially recover the image, but also introduces many artifacts. Surfaces that should be smooth look very grainy. Some patches are completely black, which further degrades the image quality. Combining BM3D with our multi-scale approach (MS-BM3D) produces an image with fewer artifacts. Surfaces appear smooth again and it is easier to recognize the original image content. Even some details are recovered: For instance part of the texture of the table cloth is discernible.



noisy  $\sigma = 50$   
PSNR: 14.77dB, SSIM: 0.44



ground truth



denoised with Wiener  
PSNR: 20.77dB, SSIM: 0.579



denoised with MS-Wiener  
PSNR: 22.99dB, SSIM: 0.731

The image “Barbara” has been corrupted with AWGN ( $\sigma = 50$ ) and denoised with Wiener and MS-Wiener. The image produced by MS-Wiener looks much smoother than the one produced by Wiener (without multi-scale extension).



noisy  $\sigma = 50$   
PSNR: 14.77dB, SSIM: 0.44



ground truth



denoised with KSVD  
PSNR: 25.35dB, SSIM: 0.791



denoised with MS-KSVD  
PSNR: 26.08dB, SSIM: 0.842

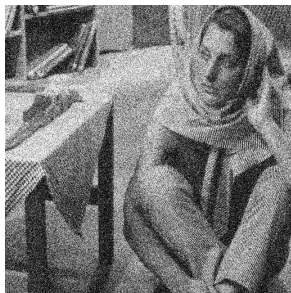
The image “Barbara” has been corrupted with AWGN ( $\sigma = 50$ ) and denoised with KSVD and MS-KSVD. With KSVD, regions of the image that should be smooth appear “wavy”. These low-frequency artifacts are due to the fact that KSVD denoises images patch by patch: Adding Gaussian noise with mean 0 will result in noise vectors with a non-zero average value on small patches. The smaller the patch size, the more dramatic this effect. Applying our multi-scale approach (MS-KSVD) reduces this effect: Few artifacts are visible in the smooth regions of the image, yet fine details have not been deteriorated.



## 6 Visual comparison on all images

We now display the images produced by the nine denoising algorithms in the plain and multi-scale settings (i.e. plain vs. our approach) for all images in the test set. We will use three different noise levels:  $\sigma = 50$ ,  $\sigma = 90$  and  $\sigma = 130$ . We report the PSNR and SSIM of each image.

Image "Barbara" with  $\sigma = 50$



noisy

PSNR:14.77dB, SSIM:0.444



ground truth



KSVD

PSNR:25.35dB, SSIM:0.791



MS-KSVD

PSNR:26.08dB, SSIM:0.842



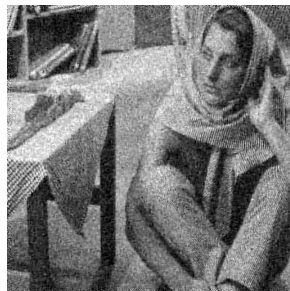
FoE

PSNR:23.63dB, SSIM:0.785



MS-FoE

PSNR:23.34dB, SSIM:0.764



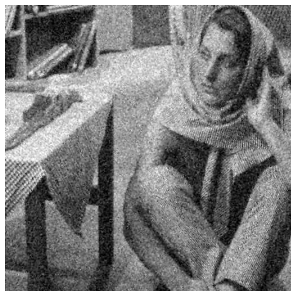
BRFoE

PSNR:21.34dB, SSIM:0.606



MS-BRFoE

PSNR:22.71dB, SSIM:0.707



Wiener

PSNR:20.77dB, SSIM:0.579



MS-Wiener

PSNR:22.99dB, SSIM:0.731



BilateralFiltering

PSNR:23.10dB, SSIM:0.733



MS-BilateralFiltering

PSNR:23.19dB, SSIM:0.734



BM3D

PSNR:27.30dB, SSIM:0.875



MS-BM3D

PSNR:27.19dB, SSIM:0.871



BLS-GSM

PSNR:24.42dB, SSIM:0.797



MS-BLS-GSM

PSNR:24.42dB, SSIM:0.797



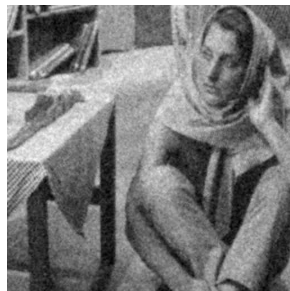
TV

PSNR:23.17dB, SSIM:0.747



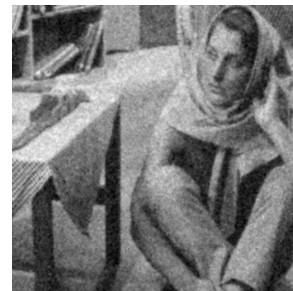
MS-TV

PSNR:23.09dB, SSIM:0.739



Stochastic

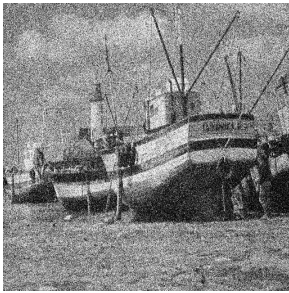
PSNR:22.66dB, SSIM:0.669



MS-Stochastic

PSNR:22.66dB, SSIM:0.669

Image "Boat" with  $\sigma = 50$

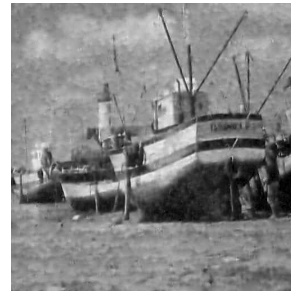


noisy

PSNR:14.59dB, SSIM:0.406



ground truth



KSVD

PSNR:25.79dB, SSIM:0.760



MS-KSVD

PSNR:26.32dB, SSIM:0.797



FoE

PSNR:25.38dB, SSIM:0.769



MS-FoE

PSNR:25.71dB, SSIM:0.792



BRFoE

PSNR:21.97dB, SSIM:0.596



MS-BRFoE

PSNR:24.64dB, SSIM:0.732



Wiener

PSNR:21.41dB, SSIM:0.565



MS-Wiener

PSNR:24.98dB, SSIM:0.743



BilateralFiltering

PSNR:24.06dB, SSIM:0.712



MS-BilateralFiltering

PSNR:25.12dB, SSIM:0.743



BM3D

PSNR:26.65dB, SSIM:0.811



MS-BM3D

PSNR:26.70dB, SSIM:0.819



BLS-GSM

PSNR:26.13dB, SSIM:0.785



MS-BLS-GSM

PSNR:26.13dB, SSIM:0.785



TV

PSNR:25.03dB, SSIM:0.734



MS-TV

PSNR:25.15dB, SSIM:0.748



Stochastic

PSNR:24.38dB, SSIM:0.685



MS-Stochastic

PSNR:24.38dB, SSIM:0.685

Image "Cameraman" with  $\sigma = 50$



noisy

PSNR:14.93dB, SSIM:0.179



ground truth



KSVD

PSNR:25.44dB, SSIM:0.704



MS-KSVD

PSNR:25.44dB, SSIM:0.716



FoE

PSNR:24.63dB, SSIM:0.756



MS-FoE

PSNR:24.07dB, SSIM:0.715



BRFoE

PSNR:20.92dB, SSIM:0.449



MS-BRFoE

PSNR:22.68dB, SSIM:0.602



Wiener

PSNR:21.17dB, SSIM:0.374



MS-Wiener

PSNR:23.73dB, SSIM:0.689



BilateralFiltering

PSNR:22.51dB, SSIM:0.576



MS-BilateralFiltering

PSNR:24.30dB, SSIM:0.703



BM3D

PSNR:26.03dB, SSIM:0.777



MS-BM3D

PSNR:25.90dB, SSIM:0.770



BLS-GSM

PSNR:25.45dB, SSIM:0.725



MS-BLS-GSM

PSNR:25.45dB, SSIM:0.725



TV

PSNR:24.44dB, SSIM:0.749



MS-TV

PSNR:24.21dB, SSIM:0.743



Stochastic

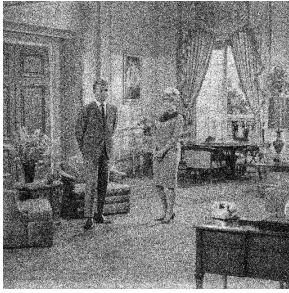
PSNR:22.45dB, SSIM:0.517



MS-Stochastic

PSNR:22.45dB, SSIM:0.517

Image "Couple" with  $\sigma = 50$



noisy

PSNR:14.58dB, SSIM:0.433



ground truth



KSVD

PSNR:25.43dB, SSIM:0.760



MS-KSVD

PSNR:25.90dB, SSIM:0.792



FoE

PSNR:25.00dB, SSIM:0.749



MS-FoE

PSNR:25.59dB, SSIM:0.796



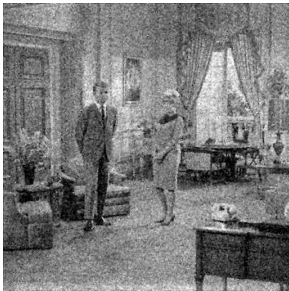
BRFoE

PSNR:22.01dB, SSIM:0.627



MS-BRFoE

PSNR:24.51dB, SSIM:0.743



Wiener

PSNR:21.42dB, SSIM:0.593



MS-Wiener

PSNR:24.67dB, SSIM:0.731



BilateralFiltering

PSNR:23.97dB, SSIM:0.701



MS-BilateralFiltering

PSNR:24.73dB, SSIM:0.726



BM3D

PSNR:26.43dB, SSIM:0.812



MS-BM3D

PSNR:26.55dB, SSIM:0.825



BLS-GSM

PSNR:25.84dB, SSIM:0.779



MS-BLS-GSM

PSNR:25.84dB, SSIM:0.779



TV

PSNR:24.62dB, SSIM:0.708



MS-TV

PSNR:24.81dB, SSIM:0.726



Stochastic

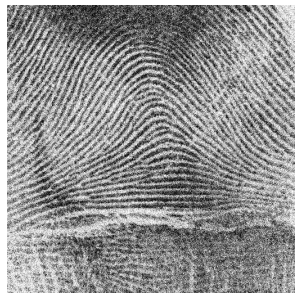
PSNR:24.35dB, SSIM:0.698



MS-Stochastic

PSNR:24.35dB, SSIM:0.698

Image “Fingerprint” with  $\sigma = 50$

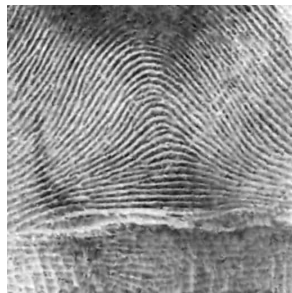


noisy

PSNR:14.71dB, SSIM:0.776

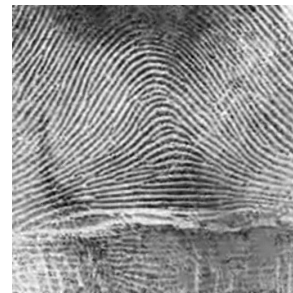


ground truth



KSVD

PSNR:23.19dB, SSIM:0.857



MS-KSVD

PSNR:24.08dB, SSIM:0.896



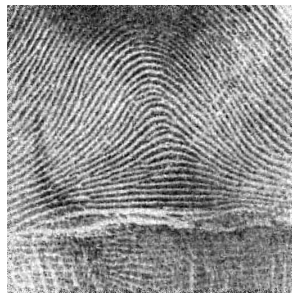
FoE

PSNR:22.57dB, SSIM:0.821



MS-FoE

PSNR:23.37dB, SSIM:0.895



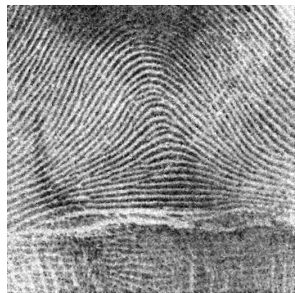
BRFoE

PSNR:21.87dB, SSIM:0.888



MS-BRFoE

PSNR:22.93dB, SSIM:0.861



Wiener

PSNR:21.02dB, SSIM:0.872



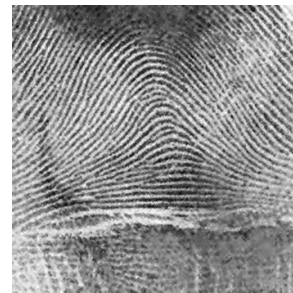
MS-Wiener

PSNR:23.03dB, SSIM:0.872



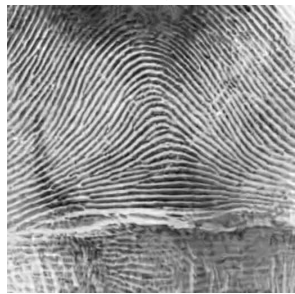
BilateralFiltering

PSNR:19.33dB, SSIM:0.635



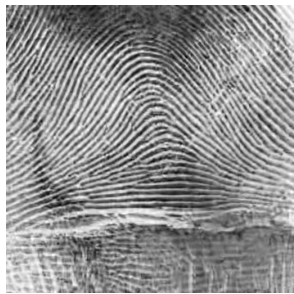
MS-BilateralFiltering

PSNR:23.18dB, SSIM:0.874



BM3D

PSNR:24.49dB, SSIM:0.904



MS-BM3D

PSNR:24.45dB, SSIM:0.908



BLS-GSM

PSNR:23.22dB, SSIM:0.861



MS-BLS-GSM

PSNR:23.22dB, SSIM:0.861



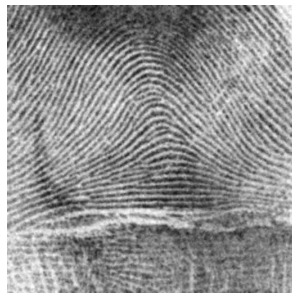
TV

PSNR:20.91dB, SSIM:0.722



MS-TV

PSNR:21.78dB, SSIM:0.795



Stochastic

PSNR:22.42dB, SSIM:0.851



MS-Stochastic

PSNR:22.42dB, SSIM:0.851

Image "Flintstones" with  $\sigma = 50$



noisy

PSNR:15.20dB, SSIM:0.647



ground truth



KSVD

PSNR:24.24dB, SSIM:0.884



MS-KSVD

PSNR:24.05dB, SSIM:0.884



FoE

PSNR:23.35dB, SSIM:0.869



MS-FoE

PSNR:23.19dB, SSIM:0.855



BRFoE

PSNR:21.84dB, SSIM:0.791



MS-BRFoE

PSNR:22.40dB, SSIM:0.839



Wiener

PSNR:20.88dB, SSIM:0.768



MS-Wiener

PSNR:22.90dB, SSIM:0.849



BilateralFiltering

PSNR:19.72dB, SSIM:0.732



MS-BilateralFiltering

PSNR:23.02dB, SSIM:0.846



BM3D

PSNR:25.04dB, SSIM:0.911



MS-BM3D

PSNR:24.60dB, SSIM:0.899



BLS-GSM

PSNR:23.93dB, SSIM:0.880



MS-BLS-GSM

PSNR:23.93dB, SSIM:0.880



TV

PSNR:22.10dB, SSIM:0.833



MS-TV

PSNR:22.40dB, SSIM:0.851



Stochastic

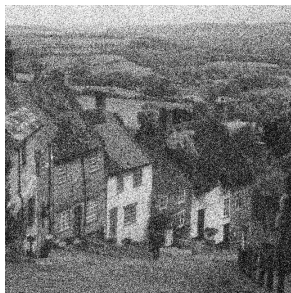
PSNR:20.97dB, SSIM:0.784



MS-Stochastic

PSNR:20.97dB, SSIM:0.784

Image "Hill" with  $\sigma = 50$



noisy

PSNR:14.67dB, SSIM:0.388



ground truth



KSVD

PSNR:26.22dB, SSIM:0.740



MS-KSVD

PSNR:26.76dB, SSIM:0.769



FoE

PSNR:26.07dB, SSIM:0.745



MS-FoE

PSNR:26.54dB, SSIM:0.772



BRFoE

PSNR:22.36dB, SSIM:0.601



MS-BRFoE

PSNR:25.42dB, SSIM:0.728



Wiener

PSNR:21.61dB, SSIM:0.564



MS-Wiener

PSNR:25.77dB, SSIM:0.729



BilateralFiltering

PSNR:25.46dB, SSIM:0.723



MS-BilateralFiltering

PSNR:25.80dB, SSIM:0.722



BM3D

PSNR:27.05dB, SSIM:0.787



MS-BM3D

PSNR:27.18dB, SSIM:0.795



BLS-GSM

PSNR:26.65dB, SSIM:0.762



MS-BLS-GSM

PSNR:26.65dB, SSIM:0.762



TV

PSNR:25.83dB, SSIM:0.703



MS-TV

PSNR:25.86dB, SSIM:0.709



Stochastic

PSNR:25.38dB, SSIM:0.699



MS-Stochastic

PSNR:25.38dB, SSIM:0.699



Image "House" with  $\sigma = 50$



noisy

PSNR:14.56dB, SSIM:0.125



ground truth



KSVD

PSNR:27.52dB, SSIM:0.733



MS-KSVD

PSNR:28.78dB, SSIM:0.781



FoE

PSNR:27.29dB, SSIM:0.774



MS-FoE

PSNR:27.72dB, SSIM:0.763



BRFoE

PSNR:21.43dB, SSIM:0.418



MS-BRFoE

PSNR:25.23dB, SSIM:0.632



Wiener

PSNR:21.47dB, SSIM:0.332



MS-Wiener

PSNR:26.55dB, SSIM:0.722



BilateralFiltering

PSNR:25.05dB, SSIM:0.599



MS-BilateralFiltering

PSNR:26.95dB, SSIM:0.720



BM3D

PSNR:29.61dB, SSIM:0.806



MS-BM3D

PSNR:29.61dB, SSIM:0.804



BLS-GSM

PSNR:28.35dB, SSIM:0.759



MS-BLS-GSM

PSNR:28.35dB, SSIM:0.759



TV

PSNR:27.46dB, SSIM:0.784



MS-TV

PSNR:27.39dB, SSIM:0.783



Stochastic

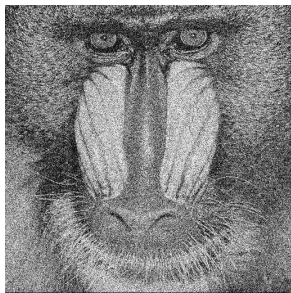
PSNR:25.45dB, SSIM:0.557



MS-Stochastic

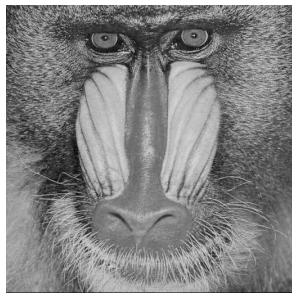
PSNR:25.45dB, SSIM:0.557

Image "Baboon" with  $\sigma = 50$

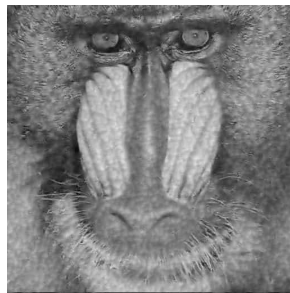


noisy

PSNR:14.55dB, SSIM:0.513

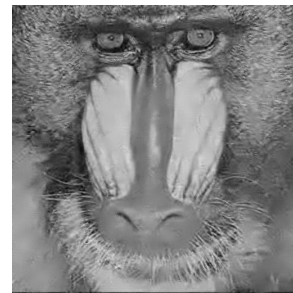


ground truth



KSVD

PSNR:22.10dB, SSIM:0.669



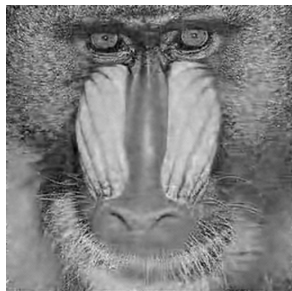
MS-KSVD

PSNR:22.39dB, SSIM:0.701



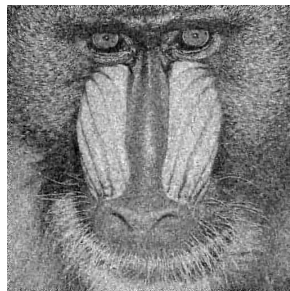
FoE

PSNR:21.76dB, SSIM:0.655



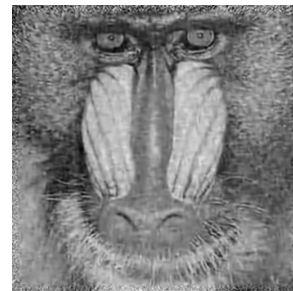
MS-FoE

PSNR:21.77dB, SSIM:0.705



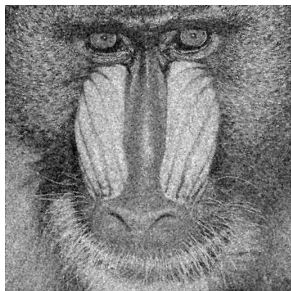
BRFoE

PSNR:20.72dB, SSIM:0.663



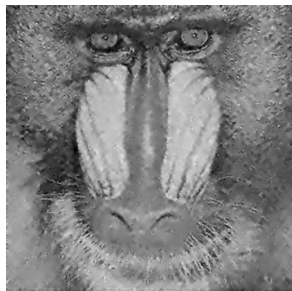
MS-BRFoE

PSNR:21.23dB, SSIM:0.657



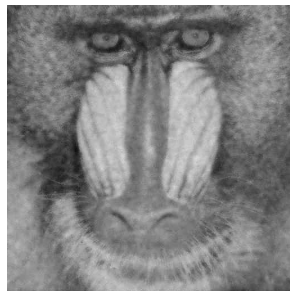
Wiener

PSNR:20.18dB, SSIM:0.640



MS-Wiener

PSNR:21.42dB, SSIM:0.660



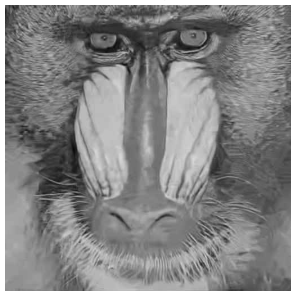
BilateralFiltering

PSNR:21.39dB, SSIM:0.613



MS-BilateralFiltering

PSNR:21.55dB, SSIM:0.657



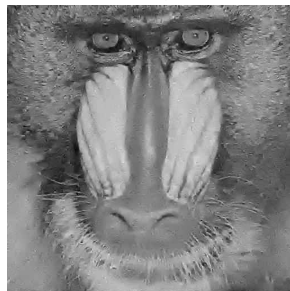
BM3D

PSNR:22.56dB, SSIM:0.713



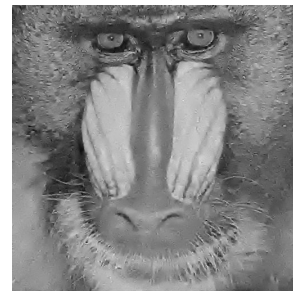
MS-BM3D

PSNR:22.57dB, SSIM:0.723



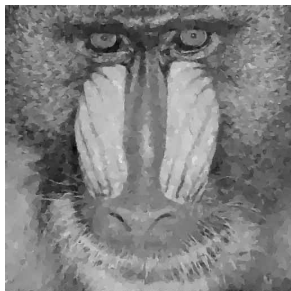
BLS-GSM

PSNR:22.21dB, SSIM:0.680



MS-BLS-GSM

PSNR:22.21dB, SSIM:0.680



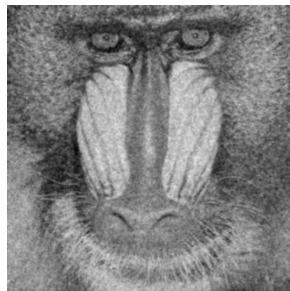
TV

PSNR:21.60dB, SSIM:0.638



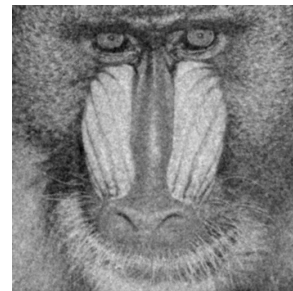
MS-TV

PSNR:21.60dB, SSIM:0.628



Stochastic

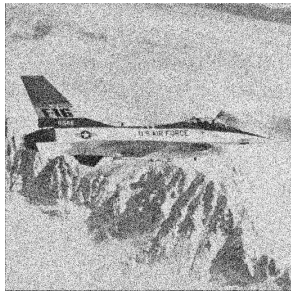
PSNR:21.31dB, SSIM:0.658



MS-Stochastic

PSNR:21.31dB, SSIM:0.658

Image "F16" with  $\sigma = 50$



noisy

PSNR:15.09dB, SSIM:0.335



ground truth



KSVD

PSNR:27.04dB, SSIM:0.791



MS-KSVD

PSNR:27.91dB, SSIM:0.870



FoE

PSNR:27.17dB, SSIM:0.858



MS-FoE

PSNR:27.20dB, SSIM:0.856



BRFoE

PSNR:22.43dB, SSIM:0.519



MS-BRFoE

PSNR:25.58dB, SSIM:0.719



Wiener

PSNR:21.75dB, SSIM:0.489



MS-Wiener

PSNR:26.36dB, SSIM:0.807



BilateralFiltering

PSNR:24.98dB, SSIM:0.753



MS-BilateralFiltering

PSNR:26.64dB, SSIM:0.828



BM3D

PSNR:28.49dB, SSIM:0.876



MS-BM3D

PSNR:28.40dB, SSIM:0.871



BLS-GSM

PSNR:27.76dB, SSIM:0.845



MS-BLS-GSM

PSNR:27.76dB, SSIM:0.845



TV

PSNR:26.42dB, SSIM:0.836



MS-TV

PSNR:26.71dB, SSIM:0.847



Stochastic

PSNR:25.21dB, SSIM:0.654



MS-Stochastic

PSNR:25.21dB, SSIM:0.654

Image “Lena” with  $\sigma = 50$



noisy

PSNR:14.61dB, SSIM:0.354



ground truth



KSVD

PSNR:27.39dB, SSIM:0.784



MS-KSVD

PSNR:28.58dB, SSIM:0.864



FoE

PSNR:27.29dB, SSIM:0.832



MS-FoE

PSNR:27.96dB, SSIM:0.841



BRFoE

PSNR:22.32dB, SSIM:0.548



MS-BRFoE

PSNR:26.09dB, SSIM:0.737



Wiener

PSNR:21.76dB, SSIM:0.518



MS-Wiener

PSNR:27.13dB, SSIM:0.802



BilateralFiltering

PSNR:25.88dB, SSIM:0.766



MS-BilateralFiltering

PSNR:27.08dB, SSIM:0.796



BM3D

PSNR:28.98dB, SSIM:0.865



MS-BM3D

PSNR:29.04dB, SSIM:0.870



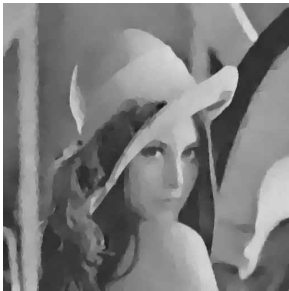
BLS-GSM

PSNR:28.17dB, SSIM:0.842



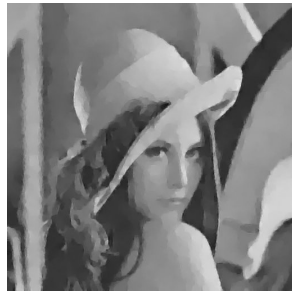
MS-BLS-GSM

PSNR:28.17dB, SSIM:0.842



TV

PSNR:26.81dB, SSIM:0.807



MS-TV

PSNR:27.05dB, SSIM:0.816



Stochastic

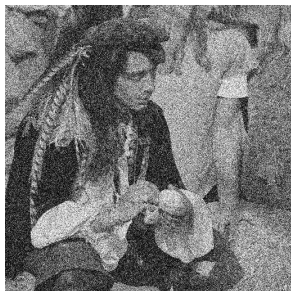
PSNR:25.89dB, SSIM:0.681



MS-Stochastic

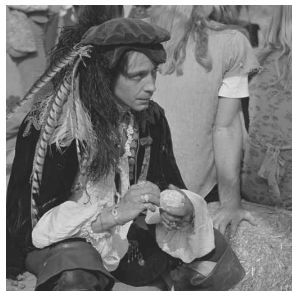
PSNR:25.89dB, SSIM:0.681

Image “Man” with  $\sigma = 50$



noisy

PSNR:14.66dB, SSIM:0.404



ground truth



KSVD

PSNR:25.85dB, SSIM:0.747



MS-KSVD

PSNR:26.36dB, SSIM:0.786



FoE

PSNR:25.54dB, SSIM:0.753



MS-FoE

PSNR:26.03dB, SSIM:0.778



BRFoE

PSNR:22.07dB, SSIM:0.604



MS-BRFoE

PSNR:25.00dB, SSIM:0.734



Wiener

PSNR:21.55dB, SSIM:0.572



MS-Wiener

PSNR:25.49dB, SSIM:0.747



BilateralFiltering

PSNR:24.83dB, SSIM:0.728



MS-BilateralFiltering

PSNR:25.59dB, SSIM:0.744



BM3D

PSNR:26.76dB, SSIM:0.800



MS-BM3D

PSNR:26.73dB, SSIM:0.802



BLS-GSM

PSNR:26.34dB, SSIM:0.777



MS-BLS-GSM

PSNR:26.34dB, SSIM:0.777



TV

PSNR:25.54dB, SSIM:0.730



MS-TV

PSNR:25.76dB, SSIM:0.745



Stochastic

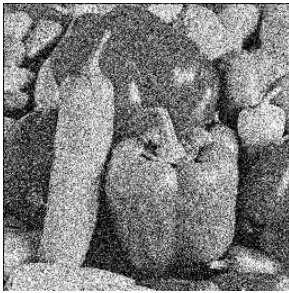
PSNR:25.01dB, SSIM:0.700



MS-Stochastic

PSNR:25.01dB, SSIM:0.700

Image "Peppers" with  $\sigma = 50$

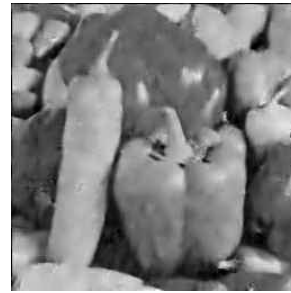


noisy

PSNR:14.67dB, SSIM:0.167

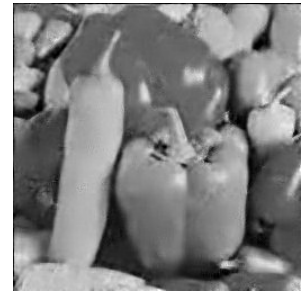


ground truth



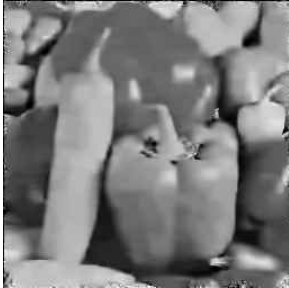
KSVD

PSNR:25.98dB, SSIM:0.762



MS-KSVD

PSNR:26.12dB, SSIM:0.766



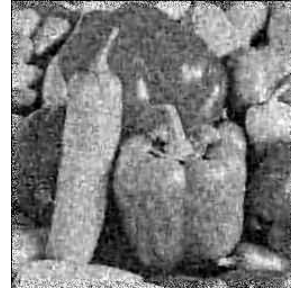
FoE

PSNR:25.41dB, SSIM:0.769



MS-FoE

PSNR:24.27dB, SSIM:0.743



BRFoE

PSNR:21.41dB, SSIM:0.506



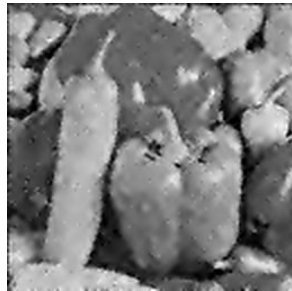
MS-BRFoE

PSNR:23.42dB, SSIM:0.689



Wiener

PSNR:21.35dB, SSIM:0.420



MS-Wiener

PSNR:23.82dB, SSIM:0.716



BilateralFiltering

PSNR:22.95dB, SSIM:0.637



MS-BilateralFiltering

PSNR:24.12dB, SSIM:0.692



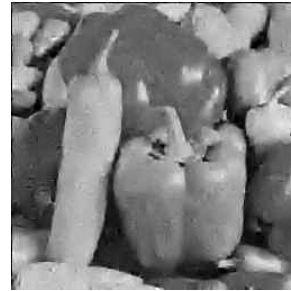
BM3D

PSNR:26.72dB, SSIM:0.794



MS-BM3D

PSNR:26.57dB, SSIM:0.786



BLS-GSM

PSNR:26.08dB, SSIM:0.760



MS-BLS-GSM

PSNR:26.08dB, SSIM:0.760



TV

PSNR:24.52dB, SSIM:0.747



MS-TV

PSNR:24.71dB, SSIM:0.753



Stochastic

PSNR:23.16dB, SSIM:0.625



MS-Stochastic

PSNR:23.16dB, SSIM:0.625

Image "Barbara" with  $\sigma = 90$



noisy

PSNR:10.83dB, SSIM:0.242



ground truth



KSVD

PSNR:21.73dB, SSIM:0.609



MS-KSVD

PSNR:22.61dB, SSIM:0.701



FoE

PSNR:21.54dB, SSIM:0.668



MS-FoE

PSNR:22.07dB, SSIM:0.682



BRFoE

PSNR:17.42dB, SSIM:0.395



MS-BRFoE

PSNR:21.70dB, SSIM:0.639



Wiener

PSNR:16.81dB, SSIM:0.373



MS-Wiener

PSNR:21.90dB, SSIM:0.649



BilateralFiltering

PSNR:21.93dB, SSIM:0.632



MS-BilateralFiltering

PSNR:21.89dB, SSIM:0.635



BM3D

PSNR:24.17dB, SSIM:0.759



MS-BM3D

PSNR:24.24dB, SSIM:0.765



BLS-GSM

PSNR:22.42dB, SSIM:0.685



MS-BLS-GSM

PSNR:22.47dB, SSIM:0.687



TV

PSNR:21.94dB, SSIM:0.664



MS-TV

PSNR:21.87dB, SSIM:0.658



Stochastic

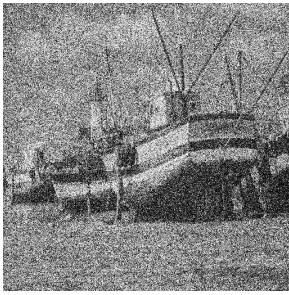
PSNR:20.46dB, SSIM:0.498



MS-Stochastic

PSNR:21.72dB, SSIM:0.611

Image "Boat" with  $\sigma = 90$

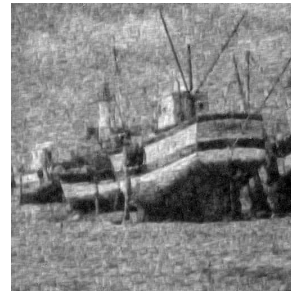


noisy

PSNR:10.68dB, SSIM:0.226



ground truth



KSVD

PSNR:22.55dB, SSIM:0.571



MS-KSVD

PSNR:24.18dB, SSIM:0.703



FoE

PSNR:22.67dB, SSIM:0.641



MS-FoE

PSNR:23.55dB, SSIM:0.691



BRFoE

PSNR:17.62dB, SSIM:0.393



MS-BRFoE

PSNR:22.53dB, SSIM:0.610



Wiener

PSNR:17.06dB, SSIM:0.366



MS-Wiener

PSNR:23.01dB, SSIM:0.638



BilateralFiltering

PSNR:22.82dB, SSIM:0.608



MS-BilateralFiltering

PSNR:23.20dB, SSIM:0.636



BM3D

PSNR:24.35dB, SSIM:0.710



MS-BM3D

PSNR:24.39dB, SSIM:0.718



BLS-GSM

PSNR:23.90dB, SSIM:0.670



MS-BLS-GSM

PSNR:23.97dB, SSIM:0.683



TV

PSNR:23.17dB, SSIM:0.640



MS-TV

PSNR:23.25dB, SSIM:0.645



Stochastic

PSNR:21.44dB, SSIM:0.502



MS-Stochastic

PSNR:22.67dB, SSIM:0.590



Image "Cameraman" with  $\sigma = 90$



noisy

PSNR:10.88dB, SSIM:0.086



ground truth



KSVD

PSNR:21.95dB, SSIM:0.467



MS-KSVD

PSNR:22.65dB, SSIM:0.640



FoE

PSNR:21.62dB, SSIM:0.669



MS-FoE

PSNR:22.06dB, SSIM:0.637



BRFoE

PSNR:17.00dB, SSIM:0.285



MS-BRFoE

PSNR:20.31dB, SSIM:0.507



Wiener

PSNR:17.01dB, SSIM:0.225



MS-Wiener

PSNR:21.34dB, SSIM:0.599



BilateralFiltering

PSNR:20.82dB, SSIM:0.515



MS-BilateralFiltering

PSNR:22.07dB, SSIM:0.618



BM3D

PSNR:23.56dB, SSIM:0.700



MS-BM3D

PSNR:23.19dB, SSIM:0.691



BLS-GSM

PSNR:22.72dB, SSIM:0.603



MS-BLS-GSM

PSNR:22.71dB, SSIM:0.615



TV

PSNR:22.33dB, SSIM:0.687



MS-TV

PSNR:22.22dB, SSIM:0.683



Stochastic

PSNR:20.41dB, SSIM:0.351



MS-Stochastic

PSNR:20.47dB, SSIM:0.519

Image "Couple" with  $\sigma = 90$

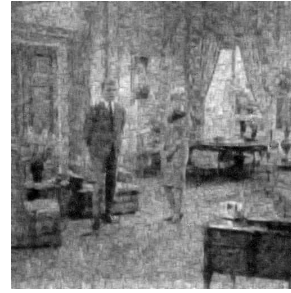


noisy

PSNR:10.64dB, SSIM:0.233



ground truth



KSVD

PSNR:22.49dB, SSIM:0.590



MS-KSVD

PSNR:23.74dB, SSIM:0.678



FoE

PSNR:22.45dB, SSIM:0.594



MS-FoE

PSNR:23.36dB, SSIM:0.675



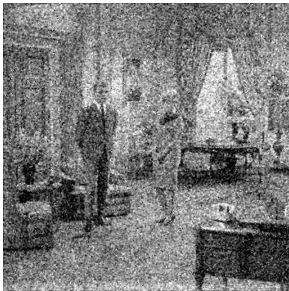
BRFoE

PSNR:17.67dB, SSIM:0.412



MS-BRFoE

PSNR:22.43dB, SSIM:0.593



Wiener

PSNR:17.01dB, SSIM:0.379



MS-Wiener

PSNR:22.75dB, SSIM:0.603



BilateralFiltering

PSNR:22.77dB, SSIM:0.601



MS-BilateralFiltering

PSNR:22.92dB, SSIM:0.607



BM3D

PSNR:23.95dB, SSIM:0.688



MS-BM3D

PSNR:24.08dB, SSIM:0.706



BLS-GSM

PSNR:23.56dB, SSIM:0.646



MS-BLS-GSM

PSNR:23.66dB, SSIM:0.663



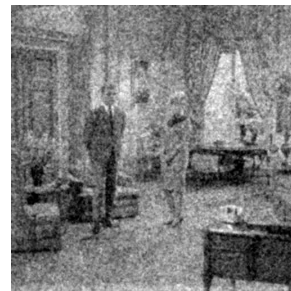
TV

PSNR:22.93dB, SSIM:0.602



MS-TV

PSNR:23.04dB, SSIM:0.613



Stochastic

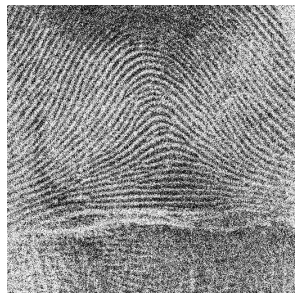
PSNR:21.43dB, SSIM:0.517



MS-Stochastic

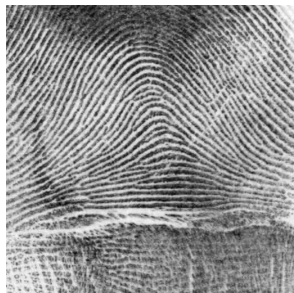
PSNR:22.61dB, SSIM:0.579

Image "Fingerprint" with  $\sigma = 90$

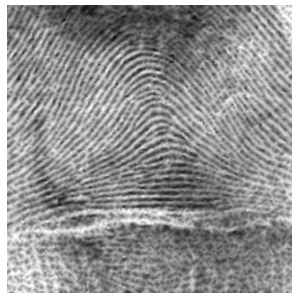


noisy

PSNR:10.80dB, SSIM:0.546

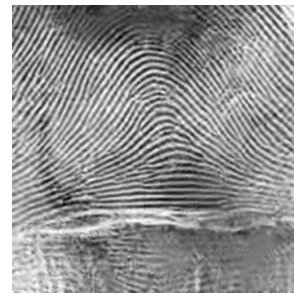


ground truth



KSVD

PSNR:20.34dB, SSIM:0.742



MS-KSVD

PSNR:21.97dB, SSIM:0.812



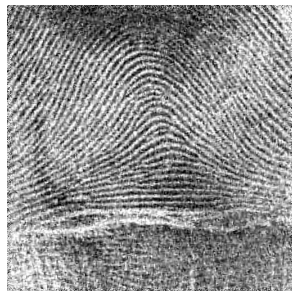
FoE

PSNR:18.36dB, SSIM:0.489



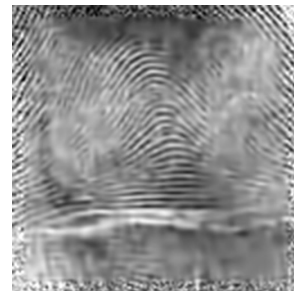
MS-FoE

PSNR:20.24dB, SSIM:0.791



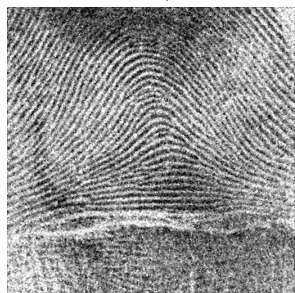
BRFoE

PSNR:17.68dB, SSIM:0.752



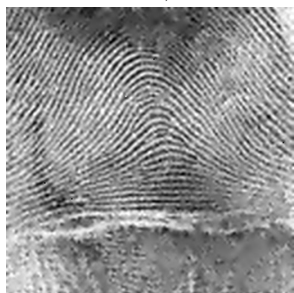
MS-BRFoE

PSNR:17.70dB, SSIM:0.401



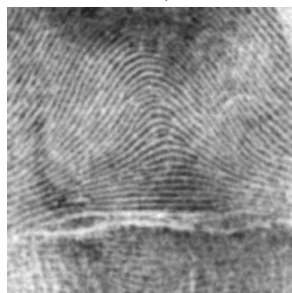
Wiener

PSNR:16.96dB, SSIM:0.725



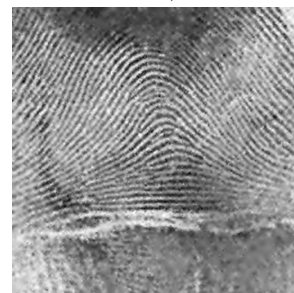
MS-Wiener

PSNR:20.62dB, SSIM:0.724



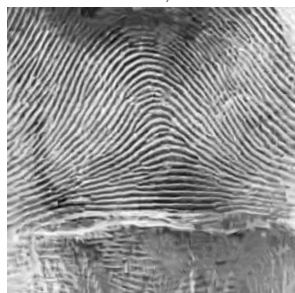
BilateralFiltering

PSNR:18.23dB, SSIM:0.510



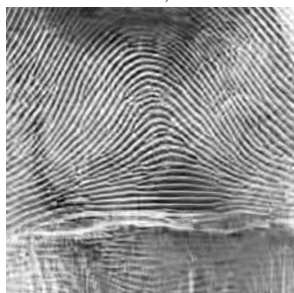
MS-BilateralFiltering

PSNR:20.40dB, SSIM:0.710



BM3D

PSNR:22.08dB, SSIM:0.818



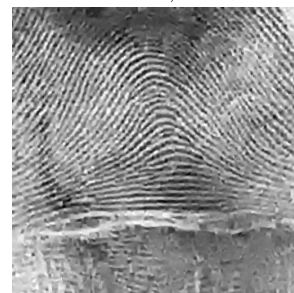
MS-BM3D

PSNR:22.09dB, SSIM:0.821



BLS-GSM

PSNR:20.34dB, SSIM:0.705



MS-BLS-GSM

PSNR:20.88dB, SSIM:0.758



TV

PSNR:18.55dB, SSIM:0.525



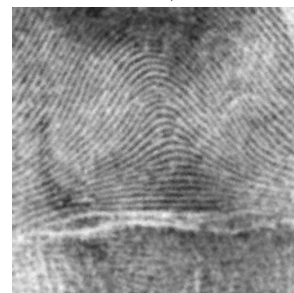
MS-TV

PSNR:19.25dB, SSIM:0.618



Stochastic

PSNR:20.38dB, SSIM:0.776



MS-Stochastic

PSNR:18.10dB, SSIM:0.491

Image "Flintstones" with  $\sigma = 90$



noisy

PSNR:11.08dB, SSIM:0.456



ground truth



KSVD

PSNR:20.64dB, SSIM:0.745



MS-KSVD

PSNR:20.59dB, SSIM:0.743



FoE

PSNR:19.57dB, SSIM:0.703



MS-FoE

PSNR:20.31dB, SSIM:0.733



BRFoE

PSNR:17.82dB, SSIM:0.638



MS-BRFoE

PSNR:17.75dB, SSIM:0.572



Wiener

PSNR:17.05dB, SSIM:0.611



MS-Wiener

PSNR:19.08dB, SSIM:0.685



BilateralFiltering

PSNR:17.94dB, SSIM:0.598



MS-BilateralFiltering

PSNR:19.98dB, SSIM:0.712



BM3D

PSNR:21.78dB, SSIM:0.811



MS-BM3D

PSNR:21.00dB, SSIM:0.767



BLS-GSM

PSNR:20.71dB, SSIM:0.758



MS-BLS-GSM

PSNR:20.90dB, SSIM:0.775



TV

PSNR:19.50dB, SSIM:0.704



MS-TV

PSNR:19.82dB, SSIM:0.729



Stochastic

PSNR:19.41dB, SSIM:0.675



MS-Stochastic

PSNR:17.62dB, SSIM:0.571

Image "Hill" with  $\sigma = 90$

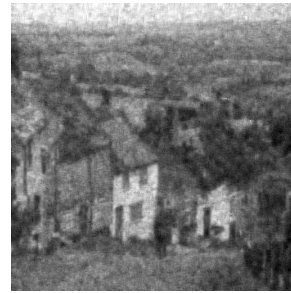


noisy

PSNR:10.77dB, SSIM:0.191



ground truth



KSVD

PSNR:23.11dB, SSIM:0.589



MS-KSVD

PSNR:25.03dB, SSIM:0.673



FoE

PSNR:23.85dB, SSIM:0.616



MS-FoE

PSNR:24.64dB, SSIM:0.670



BRFoE

PSNR:18.04dB, SSIM:0.378



MS-BRFoE

PSNR:23.82dB, SSIM:0.611



Wiener

PSNR:17.22dB, SSIM:0.342



MS-Wiener

PSNR:24.12dB, SSIM:0.615



BilateralFiltering

PSNR:24.26dB, SSIM:0.628



MS-BilateralFiltering

PSNR:24.25dB, SSIM:0.617



BM3D

PSNR:25.01dB, SSIM:0.674



MS-BM3D

PSNR:25.27dB, SSIM:0.695



BLS-GSM

PSNR:24.89dB, SSIM:0.655



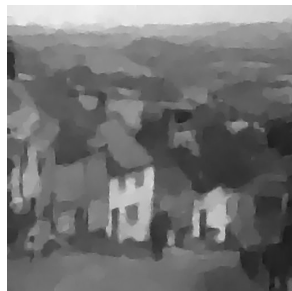
MS-BLS-GSM

PSNR:24.89dB, SSIM:0.663



TV

PSNR:23.95dB, SSIM:0.589



MS-TV

PSNR:24.11dB, SSIM:0.600



Stochastic

PSNR:21.96dB, SSIM:0.505



MS-Stochastic

PSNR:24.18dB, SSIM:0.611

Image "House" with  $\sigma = 90$

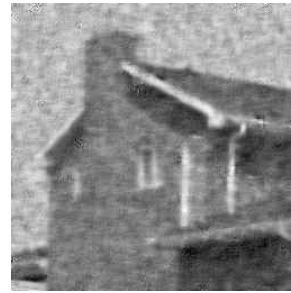


noisy

PSNR:10.74dB, SSIM:0.054

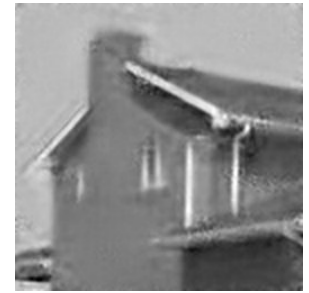


ground truth



KSVD

PSNR:23.20dB, SSIM:0.444



MS-KSVD

PSNR:25.99dB, SSIM:0.727



FoE

PSNR:23.40dB, SSIM:0.695



MS-FoE

PSNR:24.98dB, SSIM:0.707



BRFoE

PSNR:17.24dB, SSIM:0.253



MS-BRFoE

PSNR:23.16dB, SSIM:0.565



Wiener

PSNR:17.19dB, SSIM:0.192



MS-Wiener

PSNR:24.32dB, SSIM:0.679



BilateralFiltering

PSNR:23.63dB, SSIM:0.582



MS-BilateralFiltering

PSNR:24.75dB, SSIM:0.683



BM3D

PSNR:26.42dB, SSIM:0.746



MS-BM3D

PSNR:26.33dB, SSIM:0.742



BLS-GSM

PSNR:25.62dB, SSIM:0.715



MS-BLS-GSM

PSNR:25.76dB, SSIM:0.713



TV

PSNR:23.74dB, SSIM:0.712



MS-TV

PSNR:24.27dB, SSIM:0.724



Stochastic

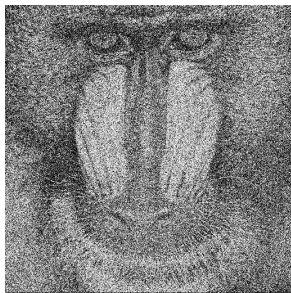
PSNR:22.05dB, SSIM:0.376



MS-Stochastic

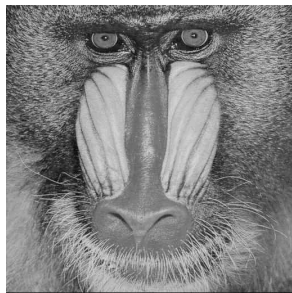
PSNR:23.52dB, SSIM:0.598

Image "Baboon" with  $\sigma = 90$

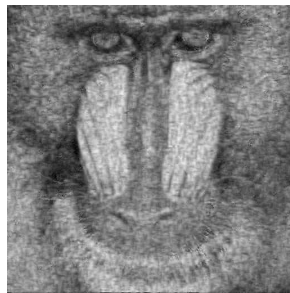


noisy

PSNR:10.62dB, SSIM:0.274

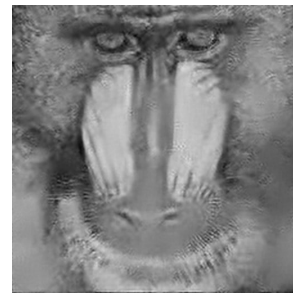


ground truth



KSVD

PSNR:20.33dB, SSIM:0.521



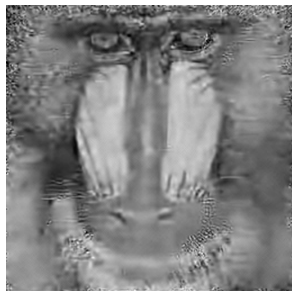
MS-KSVD

PSNR:20.57dB, SSIM:0.520



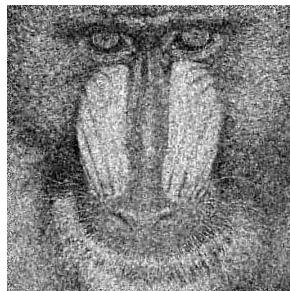
FoE

PSNR:19.97dB, SSIM:0.436



MS-FoE

PSNR:20.34dB, SSIM:0.517



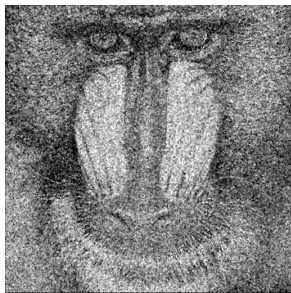
BRFoE

PSNR:17.06dB, SSIM:0.437



MS-BRFoE

PSNR:19.85dB, SSIM:0.448



Wiener

PSNR:16.41dB, SSIM:0.413



MS-Wiener

PSNR:20.05dB, SSIM:0.462



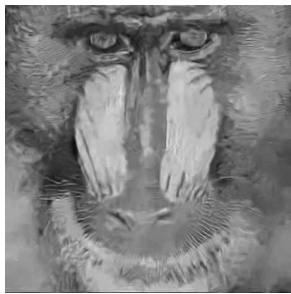
BilateralFiltering

PSNR:20.34dB, SSIM:0.499



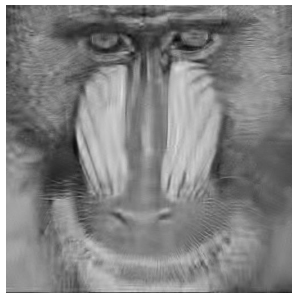
MS-BilateralFiltering

PSNR:20.19dB, SSIM:0.482



BM3D

PSNR:20.86dB, SSIM:0.542



MS-BM3D

PSNR:20.82dB, SSIM:0.525



BLS-GSM

PSNR:20.61dB, SSIM:0.513



MS-BLS-GSM

PSNR:20.60dB, SSIM:0.524



TV

PSNR:20.22dB, SSIM:0.472



MS-TV

PSNR:20.28dB, SSIM:0.465



Stochastic

PSNR:19.57dB, SSIM:0.502



MS-Stochastic

PSNR:20.06dB, SSIM:0.469

Image "F16" with  $\sigma = 90$



noisy

PSNR:11.19dB, SSIM:0.187



ground truth



KSVD

PSNR:23.46dB, SSIM:0.559



MS-KSVD

PSNR:25.07dB, SSIM:0.791



FoE

PSNR:24.05dB, SSIM:0.769



MS-FoE

PSNR:24.75dB, SSIM:0.786



BRFoE

PSNR:17.96dB, SSIM:0.330



MS-BRFoE

PSNR:23.30dB, SSIM:0.667



Wiener

PSNR:17.41dB, SSIM:0.312



MS-Wiener

PSNR:24.01dB, SSIM:0.740



BilateralFiltering

PSNR:23.50dB, SSIM:0.635



MS-BilateralFiltering

PSNR:24.30dB, SSIM:0.735



BM3D

PSNR:25.76dB, SSIM:0.802



MS-BM3D

PSNR:25.64dB, SSIM:0.802



BLS-GSM

PSNR:25.00dB, SSIM:0.736



MS-BLS-GSM

PSNR:25.09dB, SSIM:0.754



TV

PSNR:24.07dB, SSIM:0.766



MS-TV

PSNR:24.32dB, SSIM:0.777



Stochastic

PSNR:21.77dB, SSIM:0.450



MS-Stochastic

PSNR:23.31dB, SSIM:0.623



Image “Lena” with  $\sigma = 90$



noisy

PSNR:10.72dB, SSIM:0.190



ground truth



KSVD

PSNR:23.51dB, SSIM:0.597



MS-KSVD

PSNR:26.31dB, SSIM:0.789



FoE

PSNR:24.37dB, SSIM:0.749



MS-FoE

PSNR:25.40dB, SSIM:0.765



BRFoE

PSNR:17.94dB, SSIM:0.353



MS-BRFoE

PSNR:24.20dB, SSIM:0.682



Wiener

PSNR:17.21dB, SSIM:0.323



MS-Wiener

PSNR:24.96dB, SSIM:0.727



BilateralFiltering

PSNR:24.47dB, SSIM:0.665



MS-BilateralFiltering

PSNR:25.02dB, SSIM:0.709



BM3D

PSNR:26.42dB, SSIM:0.786



MS-BM3D

PSNR:26.51dB, SSIM:0.801



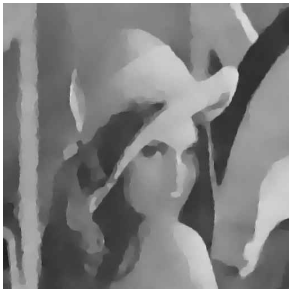
BLS-GSM

PSNR:25.88dB, SSIM:0.761



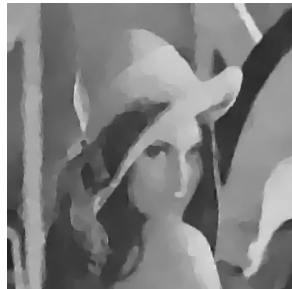
MS-BLS-GSM

PSNR:25.84dB, SSIM:0.754



TV

PSNR:24.58dB, SSIM:0.735



MS-TV

PSNR:24.98dB, SSIM:0.748



Stochastic

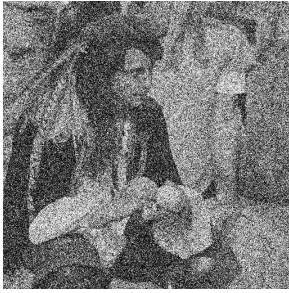
PSNR:22.18dB, SSIM:0.482



MS-Stochastic

PSNR:24.41dB, SSIM:0.653

Image “Man” with  $\sigma = 90$



noisy

PSNR:10.74dB, SSIM:0.212



ground truth



KSVD

PSNR:22.70dB, SSIM:0.593



MS-KSVD

PSNR:24.31dB, SSIM:0.680



FoE

PSNR:22.99dB, SSIM:0.629



MS-FoE

PSNR:23.86dB, SSIM:0.673



BRFoE

PSNR:17.77dB, SSIM:0.391



MS-BRFoE

PSNR:23.08dB, SSIM:0.620



Wiener

PSNR:17.13dB, SSIM:0.361



MS-Wiener

PSNR:23.61dB, SSIM:0.639



BilateralFiltering

PSNR:23.52dB, SSIM:0.630



MS-BilateralFiltering

PSNR:23.74dB, SSIM:0.639



BM3D

PSNR:24.57dB, SSIM:0.693



MS-BM3D

PSNR:24.46dB, SSIM:0.692



BLS-GSM

PSNR:24.16dB, SSIM:0.661



MS-BLS-GSM

PSNR:24.26dB, SSIM:0.675



TV

PSNR:23.64dB, SSIM:0.632



MS-TV

PSNR:23.83dB, SSIM:0.645



Stochastic

PSNR:21.71dB, SSIM:0.512



MS-Stochastic

PSNR:23.40dB, SSIM:0.613

Image “Peppers” with  $\sigma = 90$

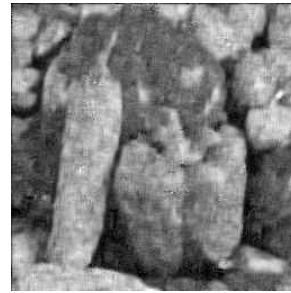


noisy

PSNR:10.75dB, SSIM:0.073

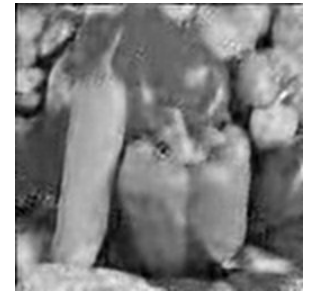


ground truth



KSVD

PSNR:22.05dB, SSIM:0.497



MS-KSVD

PSNR:22.69dB, SSIM:0.683



FoE

PSNR:22.08dB, SSIM:0.677



MS-FoE

PSNR:22.10dB, SSIM:0.654



BRFoE

PSNR:17.23dB, SSIM:0.323



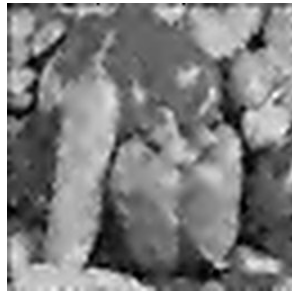
MS-BRFoE

PSNR:21.28dB, SSIM:0.619



Wiener

PSNR:16.99dB, SSIM:0.250



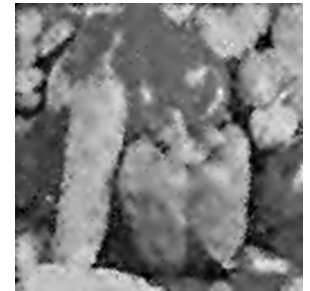
MS-Wiener

PSNR:21.70dB, SSIM:0.648



BilateralFiltering

PSNR:21.44dB, SSIM:0.604



MS-BilateralFiltering

PSNR:21.90dB, SSIM:0.639



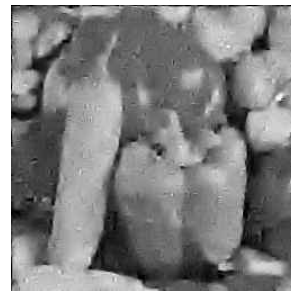
BM3D

PSNR:23.94dB, SSIM:0.707



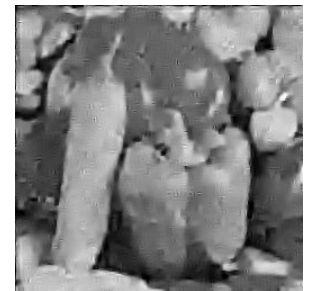
MS-BM3D

PSNR:23.48dB, SSIM:0.686



BLS-GSM

PSNR:23.12dB, SSIM:0.637



MS-BLS-GSM

PSNR:23.14dB, SSIM:0.652



TV

PSNR:21.89dB, SSIM:0.676



MS-TV

PSNR:21.78dB, SSIM:0.671



Stochastic

PSNR:20.84dB, SSIM:0.448



MS-Stochastic

PSNR:21.03dB, SSIM:0.618

Image “Barbara” with  $\sigma = 130$



noisy

PSNR:9.02dB, SSIM:0.146



ground truth



KSVD

PSNR:19.66dB, SSIM:0.498



MS-KSVD

PSNR:21.65dB, SSIM:0.643



FoE

PSNR:20.21dB, SSIM:0.593



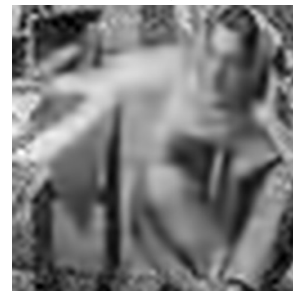
MS-FoE

PSNR:21.27dB, SSIM:0.631



BRFoE

PSNR:15.00dB, SSIM:0.278



MS-BRFoE

PSNR:20.67dB, SSIM:0.549



Wiener

PSNR:14.32dB, SSIM:0.261



MS-Wiener

PSNR:21.00dB, SSIM:0.591



BilateralFiltering

PSNR:20.99dB, SSIM:0.556



MS-BilateralFiltering

PSNR:21.03dB, SSIM:0.580



BM3D

PSNR:21.95dB, SSIM:0.653



MS-BM3D

PSNR:21.92dB, SSIM:0.664



BLS-GSM

PSNR:21.44dB, SSIM:0.612



MS-BLS-GSM

PSNR:21.52dB, SSIM:0.628



TV

PSNR:20.86dB, SSIM:0.592



MS-TV

PSNR:20.96dB, SSIM:0.596



Stochastic

PSNR:18.36dB, SSIM:0.380



MS-Stochastic

PSNR:20.81dB, SSIM:0.532

Image "Boat" with  $\sigma = 130$



noisy

PSNR:8.96dB, SSIM:0.138



ground truth



KSVD

PSNR:20.31dB, SSIM:0.460



MS-KSVD

PSNR:22.71dB, SSIM:0.618



FoE

PSNR:20.94dB, SSIM:0.560



MS-FoE

PSNR:22.28dB, SSIM:0.610



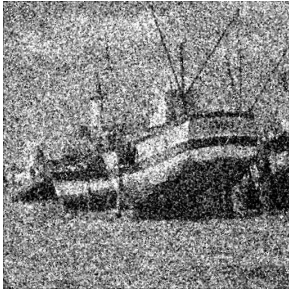
BRFoE

PSNR:15.12dB, SSIM:0.278



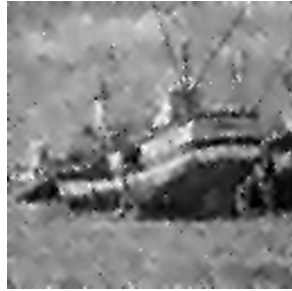
MS-BRFoE

PSNR:21.26dB, SSIM:0.513



Wiener

PSNR:14.39dB, SSIM:0.254



MS-Wiener

PSNR:21.74dB, SSIM:0.557



BilateralFiltering

PSNR:21.80dB, SSIM:0.524



MS-BilateralFiltering

PSNR:22.02dB, SSIM:0.565



BM3D

PSNR:22.72dB, SSIM:0.620



MS-BM3D

PSNR:23.01dB, SSIM:0.645



BLS-GSM

PSNR:22.56dB, SSIM:0.587



MS-BLS-GSM

PSNR:22.67dB, SSIM:0.608



TV

PSNR:21.94dB, SSIM:0.572



MS-TV

PSNR:22.15dB, SSIM:0.586



Stochastic

PSNR:18.96dB, SSIM:0.376



MS-Stochastic

PSNR:21.63dB, SSIM:0.502

Image "Cameraman" with  $\sigma = 130$



noisy

PSNR:9.02dB, SSIM:0.050



ground truth



KSVD

PSNR:19.49dB, SSIM:0.300



MS-KSVD

PSNR:21.31dB, SSIM:0.591



FoE

PSNR:19.11dB, SSIM:0.593



MS-FoE

PSNR:20.54dB, SSIM:0.584



BRFoE

PSNR:14.58dB, SSIM:0.201



MS-BRFoE

PSNR:18.67dB, SSIM:0.476



Wiener

PSNR:14.38dB, SSIM:0.158



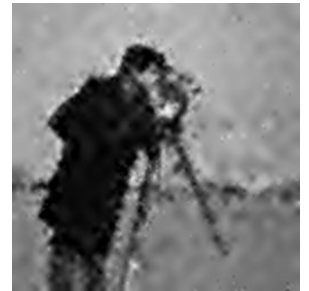
MS-Wiener

PSNR:20.04dB, SSIM:0.552



BilateralFiltering

PSNR:19.95dB, SSIM:0.483



MS-BilateralFiltering

PSNR:20.78dB, SSIM:0.577



BM3D

PSNR:21.72dB, SSIM:0.630



MS-BM3D

PSNR:21.60dB, SSIM:0.646



BLS-GSM

PSNR:21.04dB, SSIM:0.508



MS-BLS-GSM

PSNR:21.16dB, SSIM:0.594



TV

PSNR:21.11dB, SSIM:0.647



MS-TV

PSNR:20.76dB, SSIM:0.623



Stochastic

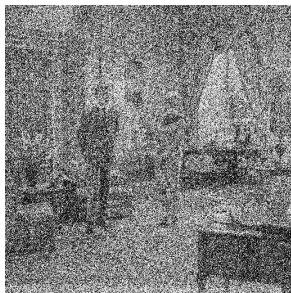
PSNR:18.41dB, SSIM:0.259



MS-Stochastic

PSNR:19.83dB, SSIM:0.441

Image "Couple" with  $\sigma = 130$



noisy

PSNR:8.94dB, SSIM:0.141

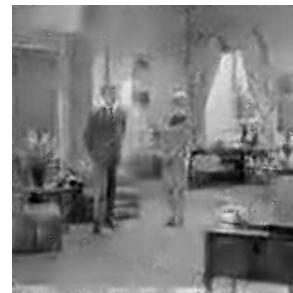


ground truth



KSVD

PSNR:20.05dB, SSIM:0.470



MS-KSVD

PSNR:22.48dB, SSIM:0.589



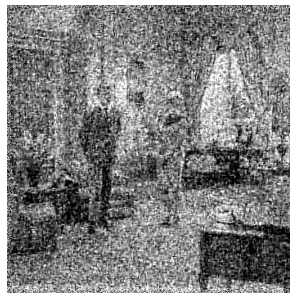
FoE

PSNR:20.66dB, SSIM:0.509



MS-FoE

PSNR:22.20dB, SSIM:0.578



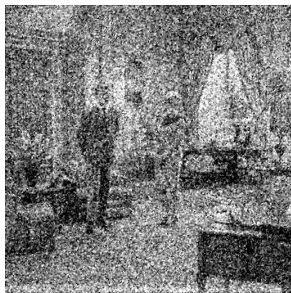
BRFoE

PSNR:15.12dB, SSIM:0.293



MS-BRFoE

PSNR:21.07dB, SSIM:0.457



Wiener

PSNR:14.30dB, SSIM:0.265



MS-Wiener

PSNR:21.62dB, SSIM:0.516



BilateralFiltering

PSNR:21.79dB, SSIM:0.523



MS-BilateralFiltering

PSNR:21.86dB, SSIM:0.529



BM3D

PSNR:22.44dB, SSIM:0.598



MS-BM3D

PSNR:22.90dB, SSIM:0.636



BLS-GSM

PSNR:22.30dB, SSIM:0.560



MS-BLS-GSM

PSNR:22.47dB, SSIM:0.582



TV

PSNR:21.91dB, SSIM:0.543



MS-TV

PSNR:21.97dB, SSIM:0.548



Stochastic

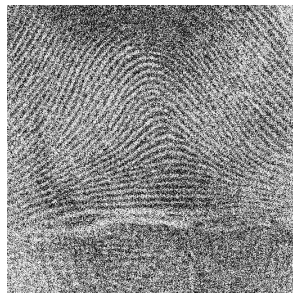
PSNR:18.91dB, SSIM:0.392



MS-Stochastic

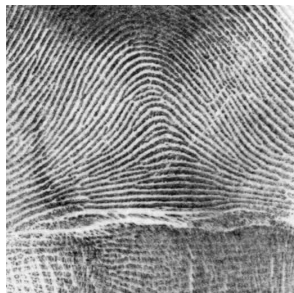
PSNR:21.61dB, SSIM:0.502

Image "Fingerprint" with  $\sigma = 130$



noisy

PSNR:9.02dB, SSIM:0.379

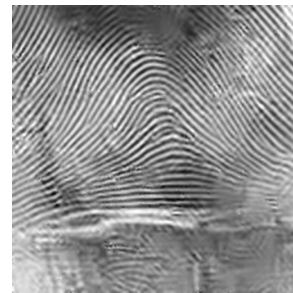


ground truth



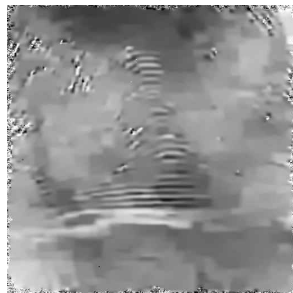
KSVD

PSNR:18.61dB, SSIM:0.667



MS-KSVD

PSNR:20.48dB, SSIM:0.713



FoE

PSNR:16.33dB, SSIM:0.227



MS-FoE

PSNR:19.35dB, SSIM:0.699



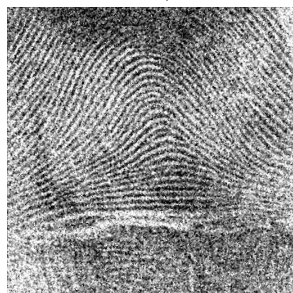
BRFoE

PSNR:15.17dB, SSIM:0.624



MS-BRFoE

PSNR:15.95dB, SSIM:0.146



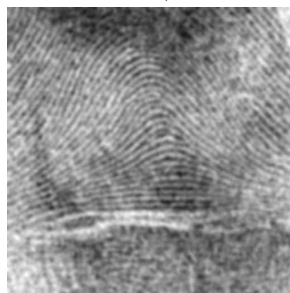
Wiener

PSNR:14.38dB, SSIM:0.591



MS-Wiener

PSNR:17.51dB, SSIM:0.416



BilateralFiltering

PSNR:17.58dB, SSIM:0.443



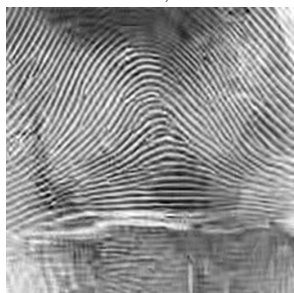
MS-BilateralFiltering

PSNR:18.36dB, SSIM:0.511



BM3D

PSNR:20.20dB, SSIM:0.718



MS-BM3D

PSNR:20.85dB, SSIM:0.755



BLS-GSM

PSNR:18.65dB, SSIM:0.562



MS-BLS-GSM

PSNR:19.37dB, SSIM:0.636



TV

PSNR:17.19dB, SSIM:0.374



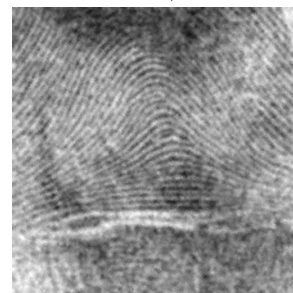
MS-TV

PSNR:18.11dB, SSIM:0.533



Stochastic

PSNR:18.29dB, SSIM:0.686



MS-Stochastic

PSNR:17.70dB, SSIM:0.469



Image "Flintstones" with  $\sigma = 130$



noisy

PSNR:9.11dB, SSIM:0.333



ground truth



KSVD

PSNR:18.59dB, SSIM:0.627



MS-KSVD

PSNR:18.76dB, SSIM:0.639



FoE

PSNR:17.16dB, SSIM:0.537



MS-FoE

PSNR:18.11dB, SSIM:0.617



BRFoE

PSNR:15.40dB, SSIM:0.532



MS-BRFoE

PSNR:15.67dB, SSIM:0.347



Wiener

PSNR:14.64dB, SSIM:0.504



MS-Wiener

PSNR:17.44dB, SSIM:0.545



BilateralFiltering

PSNR:17.31dB, SSIM:0.536



MS-BilateralFiltering

PSNR:18.28dB, SSIM:0.602



BM3D

PSNR:19.69dB, SSIM:0.715



MS-BM3D

PSNR:19.24dB, SSIM:0.682



BLS-GSM

PSNR:18.95dB, SSIM:0.652



MS-BLS-GSM

PSNR:19.08dB, SSIM:0.674



TV

PSNR:18.02dB, SSIM:0.595



MS-TV

PSNR:18.31dB, SSIM:0.624



Stochastic

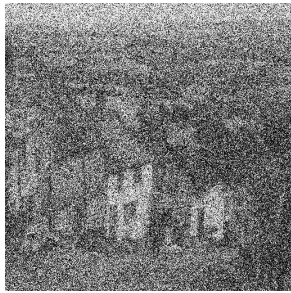
PSNR:17.89dB, SSIM:0.592



MS-Stochastic

PSNR:17.34dB, SSIM:0.535

Image "Hill" with  $\sigma = 130$



noisy

PSNR:9.01dB, SSIM:0.109



ground truth



KSVD

PSNR:20.51dB, SSIM:0.465



MS-KSVD

PSNR:23.73dB, SSIM:0.588



FoE

PSNR:22.06dB, SSIM:0.534



MS-FoE

PSNR:23.63dB, SSIM:0.589



BRFoE

PSNR:15.28dB, SSIM:0.250



MS-BRFoE

PSNR:22.62dB, SSIM:0.490



Wiener

PSNR:14.48dB, SSIM:0.224



MS-Wiener

PSNR:23.12dB, SSIM:0.543



BilateralFiltering

PSNR:23.03dB, SSIM:0.546



MS-BilateralFiltering

PSNR:23.13dB, SSIM:0.544



BM3D

PSNR:23.49dB, SSIM:0.589



MS-BM3D

PSNR:24.12dB, SSIM:0.630



BLS-GSM

PSNR:23.62dB, SSIM:0.572



MS-BLS-GSM

PSNR:23.76dB, SSIM:0.586



TV

PSNR:23.02dB, SSIM:0.536



MS-TV

PSNR:23.11dB, SSIM:0.547



Stochastic

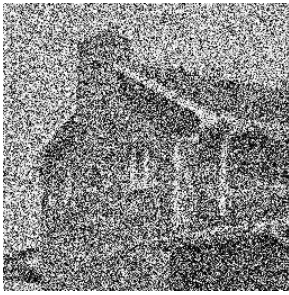
PSNR:19.21dB, SSIM:0.364



MS-Stochastic

PSNR:22.77dB, SSIM:0.521

Image "House" with  $\sigma = 130$

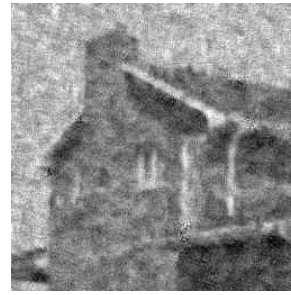


noisy

PSNR:8.97dB, SSIM:0.028



ground truth



KSVD

PSNR:20.36dB, SSIM:0.270



MS-KSVD

PSNR:24.26dB, SSIM:0.684



FoE

PSNR:21.10dB, SSIM:0.648



MS-FoE

PSNR:23.45dB, SSIM:0.665



BRFoE

PSNR:14.70dB, SSIM:0.174



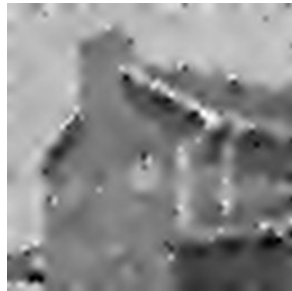
MS-BRFoE

PSNR:21.29dB, SSIM:0.554



Wiener

PSNR:14.43dB, SSIM:0.127



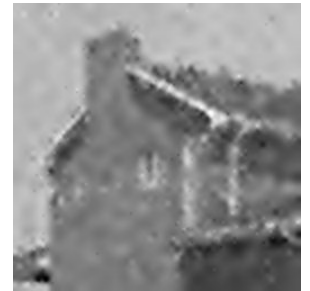
MS-Wiener

PSNR:22.40dB, SSIM:0.627



BilateralFiltering

PSNR:22.43dB, SSIM:0.571



MS-BilateralFiltering

PSNR:23.02dB, SSIM:0.646



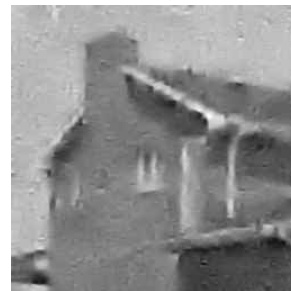
BM3D

PSNR:24.42dB, SSIM:0.686



MS-BM3D

PSNR:24.94dB, SSIM:0.711



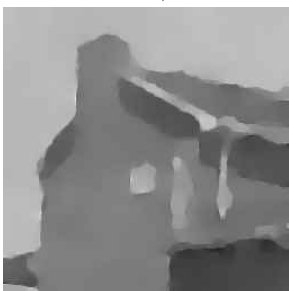
BLS-GSM

PSNR:23.94dB, SSIM:0.645



MS-BLS-GSM

PSNR:24.08dB, SSIM:0.677



TV

PSNR:22.73dB, SSIM:0.692



MS-TV

PSNR:23.28dB, SSIM:0.696



Stochastic

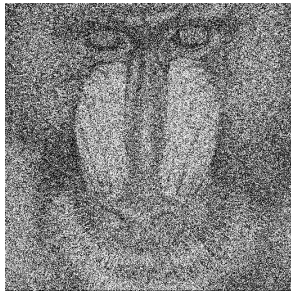
PSNR:19.24dB, SSIM:0.265



MS-Stochastic

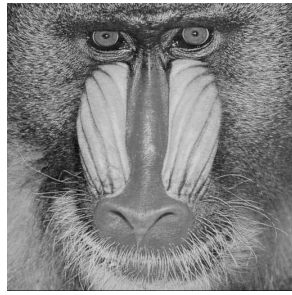
PSNR:22.26dB, SSIM:0.522

Image "Baboon" with  $\sigma = 130$

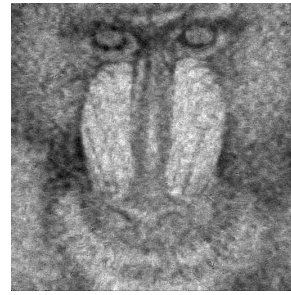


noisy

PSNR:8.96dB, SSIM:0.164

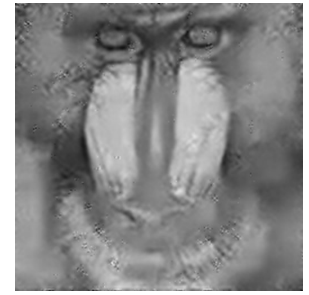


ground truth



KSVD

PSNR:18.73dB, SSIM:0.425



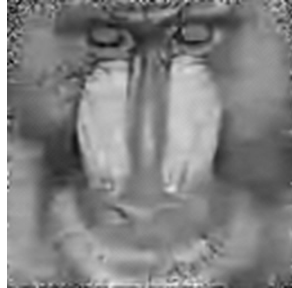
MS-KSVD

PSNR:19.90dB, SSIM:0.424



FoE

PSNR:18.98dB, SSIM:0.359



MS-FoE

PSNR:19.69dB, SSIM:0.403



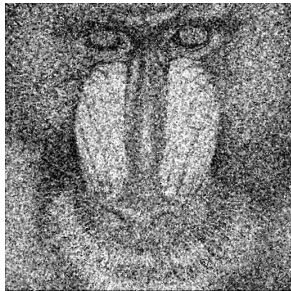
BRFoE

PSNR:14.69dB, SSIM:0.302



MS-BRFoE

PSNR:19.30dB, SSIM:0.345



Wiener

PSNR:14.00dB, SSIM:0.284



MS-Wiener

PSNR:19.55dB, SSIM:0.384



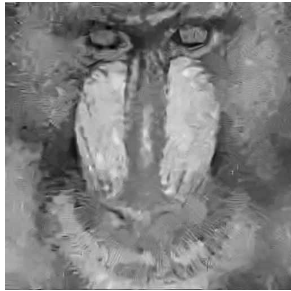
BilateralFiltering

PSNR:19.62dB, SSIM:0.425



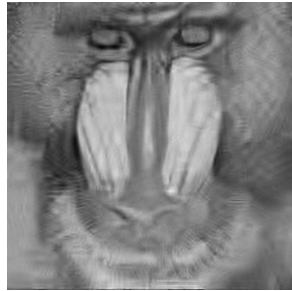
MS-BilateralFiltering

PSNR:19.65dB, SSIM:0.399



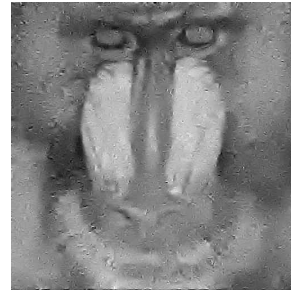
BM3D

PSNR:20.00dB, SSIM:0.453



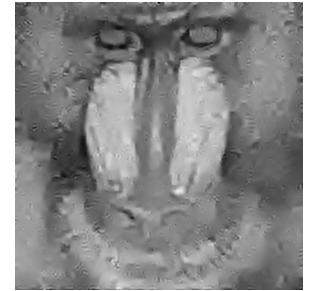
MS-BM3D

PSNR:20.12dB, SSIM:0.453



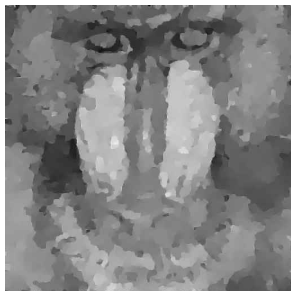
BLS-GSM

PSNR:19.92dB, SSIM:0.437



MS-BLS-GSM

PSNR:19.90dB, SSIM:0.429



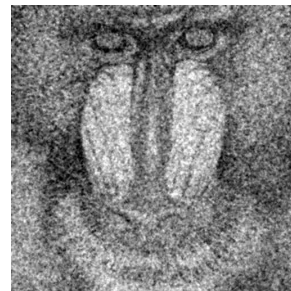
TV

PSNR:19.64dB, SSIM:0.399



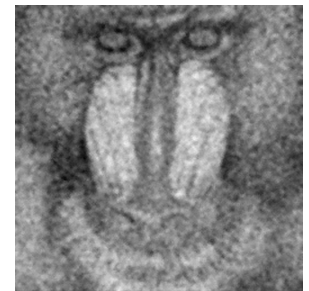
MS-TV

PSNR:19.71dB, SSIM:0.389



Stochastic

PSNR:17.76dB, SSIM:0.380



MS-Stochastic

PSNR:19.48dB, SSIM:0.413

Image "F16" with  $\sigma = 130$



noisy

PSNR:9.32dB, SSIM:0.120



ground truth



KSVD

PSNR:21.14dB, SSIM:0.440



MS-KSVD

PSNR:23.79dB, SSIM:0.758



FoE

PSNR:22.11dB, SSIM:0.708



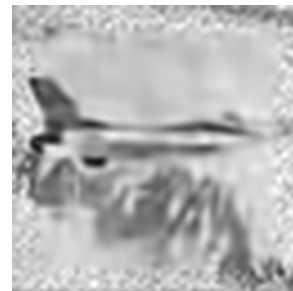
MS-FoE

PSNR:23.49dB, SSIM:0.752



BRFoE

PSNR:15.54dB, SSIM:0.245



MS-BRFoE

PSNR:21.83dB, SSIM:0.597



Wiener

PSNR:14.90dB, SSIM:0.229



MS-Wiener

PSNR:22.62dB, SSIM:0.686



BilateralFiltering

PSNR:22.59dB, SSIM:0.554



MS-BilateralFiltering

PSNR:23.13dB, SSIM:0.701



BM3D

PSNR:24.02dB, SSIM:0.741



MS-BM3D

PSNR:24.25dB, SSIM:0.760



BLS-GSM

PSNR:23.69dB, SSIM:0.682



MS-BLS-GSM

PSNR:23.73dB, SSIM:0.723



TV

PSNR:22.95dB, SSIM:0.727



MS-TV

PSNR:23.12dB, SSIM:0.732



Stochastic

PSNR:19.31dB, SSIM:0.341



MS-Stochastic

PSNR:22.33dB, SSIM:0.522

Image "Lena" with  $\sigma = 130$



noisy

PSNR:8.97dB, SSIM:0.117



ground truth



KSVD

PSNR:20.67dB, SSIM:0.478



MS-KSVD

PSNR:24.66dB, SSIM:0.738



FoE

PSNR:22.21dB, SSIM:0.686



MS-FoE

PSNR:23.96dB, SSIM:0.716



BRFoE

PSNR:15.30dB, SSIM:0.251



MS-BRFoE

PSNR:22.58dB, SSIM:0.599



Wiener

PSNR:14.49dB, SSIM:0.228



MS-Wiener

PSNR:23.43dB, SSIM:0.671



BilateralFiltering

PSNR:23.15dB, SSIM:0.580



MS-BilateralFiltering

PSNR:23.63dB, SSIM:0.656



BM3D

PSNR:24.36dB, SSIM:0.705



MS-BM3D

PSNR:25.07dB, SSIM:0.745



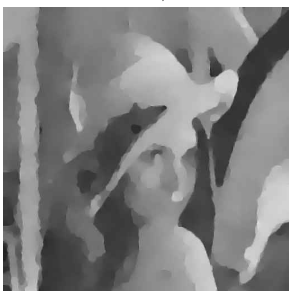
BLS-GSM

PSNR:24.26dB, SSIM:0.688



MS-BLS-GSM

PSNR:24.35dB, SSIM:0.708



TV

PSNR:23.48dB, SSIM:0.700



MS-TV

PSNR:23.76dB, SSIM:0.707



Stochastic

PSNR:19.33dB, SSIM:0.358



MS-Stochastic

PSNR:22.90dB, SSIM:0.549

Image "Man" with  $\sigma = 130$



noisy

PSNR:9.00dB, SSIM:0.130



ground truth



KSVD

PSNR:20.31dB, SSIM:0.481



MS-KSVD

PSNR:23.15dB, SSIM:0.614



FoE

PSNR:21.27dB, SSIM:0.556



MS-FoE

PSNR:22.78dB, SSIM:0.602



BRFoE

PSNR:15.21dB, SSIM:0.275



MS-BRFoE

PSNR:21.77dB, SSIM:0.510



Wiener

PSNR:14.45dB, SSIM:0.251



MS-Wiener

PSNR:22.47dB, SSIM:0.569



BilateralFiltering

PSNR:22.51dB, SSIM:0.554



MS-BilateralFiltering

PSNR:22.61dB, SSIM:0.575



BM3D

PSNR:23.16dB, SSIM:0.620



MS-BM3D

PSNR:23.39dB, SSIM:0.630



BLS-GSM

PSNR:22.89dB, SSIM:0.585



MS-BLS-GSM

PSNR:23.13dB, SSIM:0.610



TV

PSNR:22.71dB, SSIM:0.585



MS-TV

PSNR:22.66dB, SSIM:0.587



Stochastic

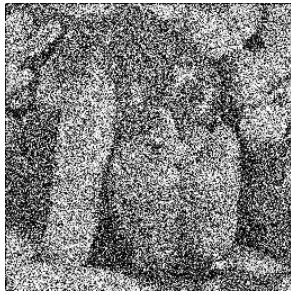
PSNR:19.12dB, SSIM:0.385



MS-Stochastic

PSNR:22.29dB, SSIM:0.532

Image “Peppers” with  $\sigma = 130$



noisy

PSNR:9.01dB, SSIM:0.039

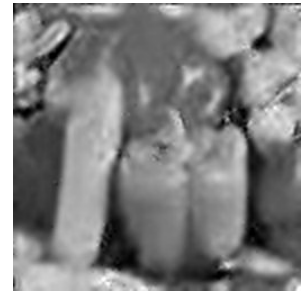


ground truth



KSVD

PSNR:19.67dB, SSIM:0.332



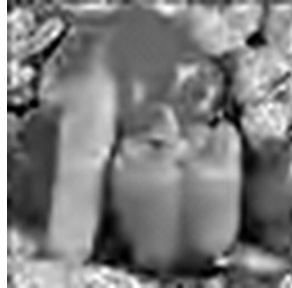
MS-KSVD

PSNR:21.10dB, SSIM:0.627



FoE

PSNR:19.54dB, SSIM:0.597



MS-FoE

PSNR:20.72dB, SSIM:0.612



BRFoE

PSNR:14.82dB, SSIM:0.224



MS-BRFoE

PSNR:19.59dB, SSIM:0.550



Wiener

PSNR:14.53dB, SSIM:0.170



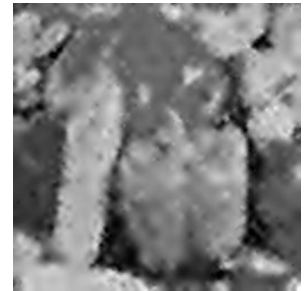
MS-Wiener

PSNR:20.34dB, SSIM:0.592



BilateralFiltering

PSNR:20.62dB, SSIM:0.587



MS-BilateralFiltering

PSNR:20.63dB, SSIM:0.595



BM3D

PSNR:21.84dB, SSIM:0.628



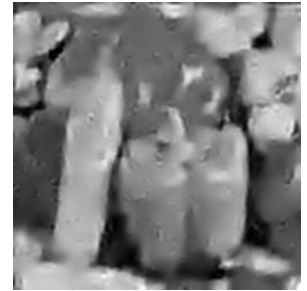
MS-BM3D

PSNR:21.41dB, SSIM:0.642



BLS-GSM

PSNR:21.39dB, SSIM:0.568



MS-BLS-GSM

PSNR:21.23dB, SSIM:0.633



TV

PSNR:19.85dB, SSIM:0.615



MS-TV

PSNR:20.22dB, SSIM:0.619



Stochastic

PSNR:18.70dB, SSIM:0.328



MS-Stochastic

PSNR:20.37dB, SSIM:0.547



## References

- [1] Estrada, F., Fleet, D., Jepson, A.: Stochastic image denoising. In: Proceedings of the British Machine Vision Conference (BMVC) (2009)
- [2] Wang, Z., Bovik, A., Sheikh, H., Simoncelli, E.: Image quality assessment: From error visibility to structural similarity. *IEEE Transactions on Image Processing* 13(4), 600–612 (2004)